

# The Equilibria of Electron Plasmas in Columbia Non-neutral Torus (CNT) Stellarator: First Results

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# Overview

- Introduce CNT
- Motivate the study of non-neutral plasmas in stellarators
- Outline the theory of non-neutral plasmas on magnetic surfaces

## **The first plasma experiments in CNT:**

- What are the immediate goals?
- Describe how plasmas are made and diagnosed
- Highlight some of the results so far



# The Columbia Non-neutral Torus (CNT)



- Only 4 circular, planar coils (Gourdon 1969)
  - Two internal interlocking (IL) coils inside vacuum chamber
  - Two poloidal field (PF) coils
- Simplest and lowest ( $<1.9$ ) aspect ratio stellarator ever built.
- **The design is not *optimized* like a modern stellarator.**
  - **Will large electric fields improve confinement?**

$B \sim 0.01-0.3 \text{ T}$

$P \geq 2 \times 10^{-10} \text{ Torr}$

Aspect Ratio  $\sim 1.9$

Volume  $\sim 0.2 \text{ m}^3$

$\iota = 0.13 - 0.21$

$\langle a \rangle = 0.15 \text{ m}$

$\langle R \rangle = 0.28 \text{ m}$



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# Why study non-neutral plasmas in a stellarator?

- Non-neutral plasmas behave differently than quasi-neutral ones do:  $e\phi \gg T \rightarrow$  electric field effects dominate.
  - The resulting ExB flow may close bad particle orbits.
    - Confinement time may improve from  $< 1$  ms to minutes.
  - The expected shear in the ExB flow may suppress turbulent transport.
- Physics is fundamentally different from previously studied non-neutral plasma traps (Penning and pure toroidal).
  - Equilibria, stability, and transport are all different (and relatively unstudied).
- May allow systematic studies of ‘exotic’ plasmas (partly neutralized and electron-positron plasmas)
  - A stellarator confines plasma of arbitrary neutralization at arbitrarily low density.



# Electron Plasma Equilibrium on Magnetic Surfaces

Low density:  $n_e \ll n_B \equiv \frac{1}{2} \epsilon_0 B^2 / m_e$

Rapid thermalization along  $\mathbf{B}$ :  $T_e = T_e(\psi)$

The density:  $n_e = N(\psi) \exp\left(\frac{e\phi}{T_e(\psi)}\right)$

$$\nabla^2 \phi = \frac{e}{\epsilon_0} N(\psi) \exp\left(\frac{e\phi}{T_e(\psi)}\right)$$

Pedersen, Boozer PRL 2002

- A 3-D code has been developed to study this equation. (Lefrancois PoP 2005)
- Equilibria described are stable to “reasonable” perturbations – **Long confinement times (seconds, minutes?) are expected.** (Boozer PoP 2004)
- Nonlinear in  $\phi$ .
- Characterized by  $\phi$ ,  $n_e$ , and  $T_e$



# Electron Plasma Experiments in CNT





# The Goals of the First Experiments in CNT

- **Learn to make small Debye length plasmas**

$$\lambda_D^2 = \frac{\epsilon_0 T_e}{en_e}$$

- Plasma definition:  $\lambda_D / a \ll 1$

- The regime we want to study:

$$\frac{e\phi}{T_e} \sim \left(\frac{a}{\lambda_D}\right)^2$$

- Confinement time:  $\tau_c \sim \left(\frac{a}{\lambda_D}\right)^4 \tau_e$

(Pedersen, Boozer PRL 2002)

- **Learn to measure plasma potential, temperature and density**

- Probe theory in non-neutral plasmas has not been well studied.

- Plasma densities, temperatures and cross field transport are low.

- **Begin to characterize equilibrium**

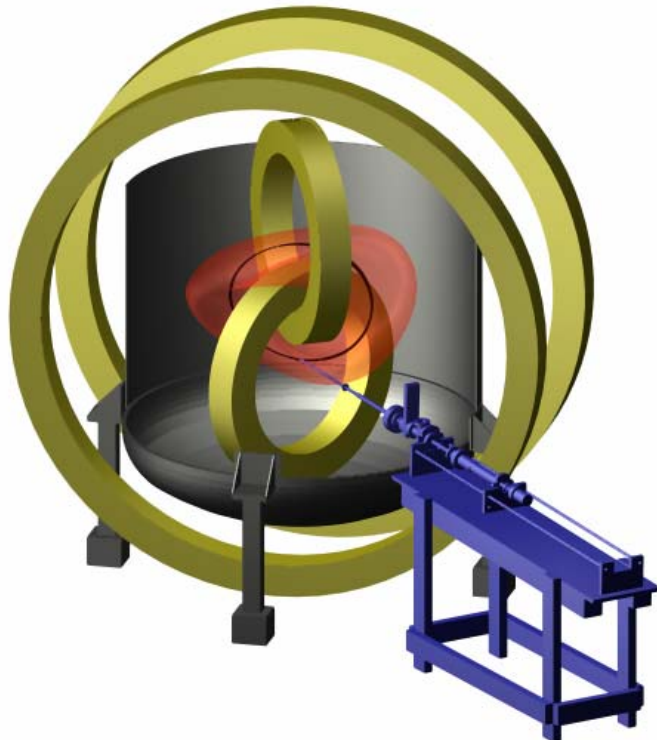
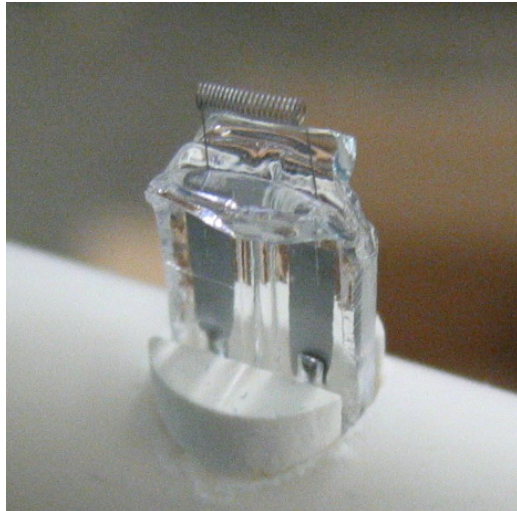
- How do confinement time, density, and temperature scale with experimental parameters (B,  $p_n$ , emitter bias, etc.)

- How well do the 3D equilibrium predictions match with experimental results?

$$\nabla^2 \phi = \frac{e}{\epsilon_0} N(\psi) \exp\left(\frac{e\phi}{T_e(\psi)}\right) \quad ?$$



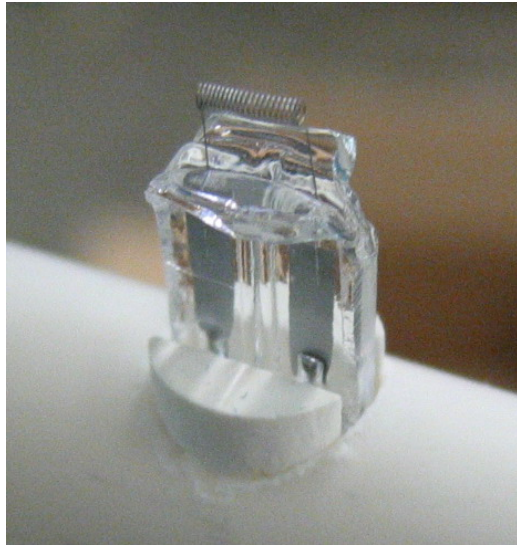
# The Electron Source



- Electrons are emitted from a heated, negatively biased tungsten filament placed in the confining region.
  - Electrons quickly fill up surface that the emitter sits on ( $\sim\mu\text{s}$ ).
  - Other surfaces are populated by cross field transport ( $\sim\text{ms}$ ).
  - Confining region fills up  $\rightarrow$  emission is space charge limited.
  - **Steady state**
    - Emission current = loss rate
    - **Our first diagnostic**
- The emitter is mounted near the end of a long alumina-oxide rod; the rod is inserted such that the emitter is placed near the magnetic axis.



# The Electron Source



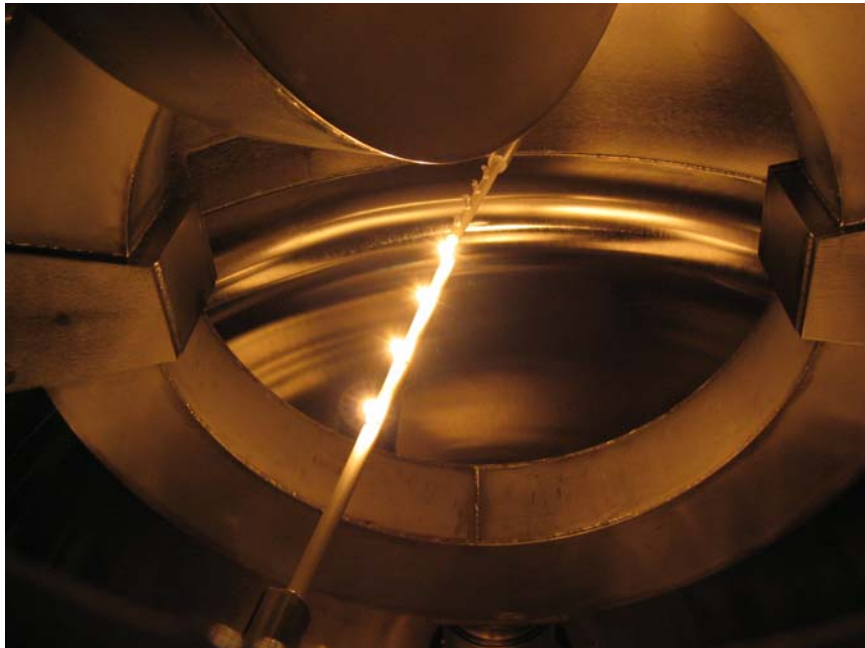
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# The Probes



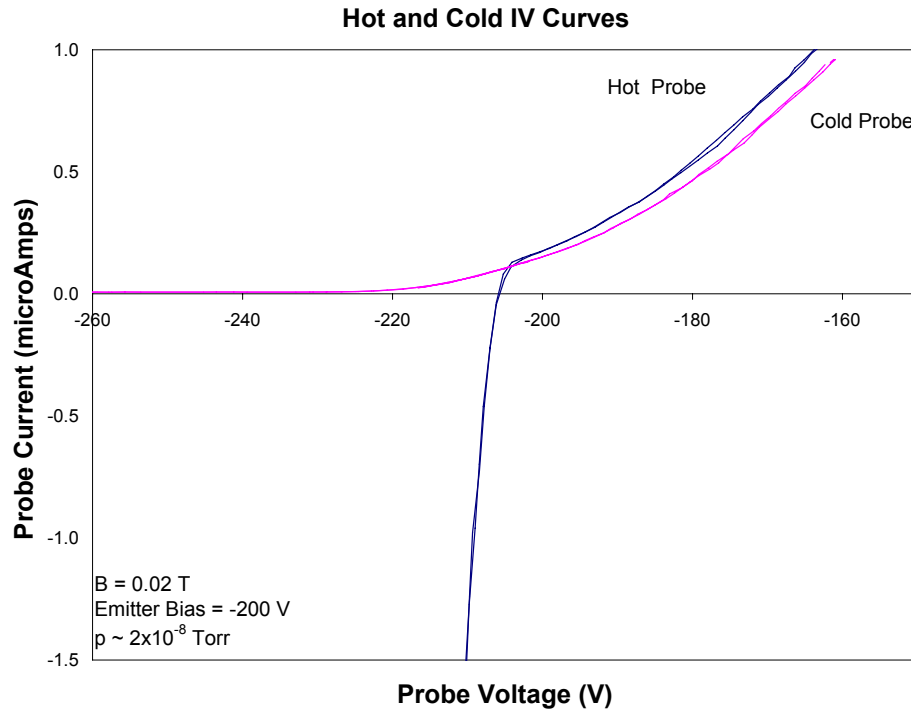
- Same type of filament as emitter
  - A cold filament is a Langmuir probe (can only collect).
  - A hot filament is a emitting probe (can emit and collect).
  - Use these probes to measure  $\phi$ ,  $n$ ,  $T$ .



- Three emitting probes are on alumina rod with the emitter; an additional eight are on a separate rod.
  - These are inserted radially into plasma so that radial profiles can be measured.



# Using the Probes



## The local plasma potential --

- The 'deviation potential' is where the cold and hot IV curves deviate.
  - This is the potential at which a hot filament starts emitting =  $\phi_{\text{plasma}}$
  - The measurement error is from the finite filament heating voltage.

## Local density and temperature—

- Measure the current-voltage characteristic of a cold filament (Langmuir)
- Electrons in a Boltzman distribution:

$$I(V_{\text{probe}}) = I_0(n_{\infty}, \sqrt{T_e}) e^{\frac{e(V_{\text{probe}} - V_{\text{plasma}})}{T_e}}$$

- Temperature and density are found by fitting the exponential region of the resulting characteristic.



Some Results:



# Total Electron Inventory and Density

**Total electron inventory from the radial potential drop across the plasma:**

$$\nabla^2\Phi = \frac{e}{\epsilon_0}n \quad \longrightarrow \quad N \approx \frac{8\pi^2\epsilon_0R(\nabla\Phi)}{e}$$

For a -150V emitter bias at B=0.05 T,  $\nabla\Phi \approx 80$  V  $\longrightarrow$   $N \approx 10^{11}$  electrons

$$\longrightarrow \quad n_e = N / V \approx 10^{12} \text{ m}^{-3}$$

**Local density measurements:**

$$n_e \approx 10^{12} \text{ m}^{-3}$$

**The CNT 3D equilibrium code predicts (from measured  $\phi$  and  $T_e$ ) :**

$$n_e \approx 10^{12} \text{ m}^{-3}$$

**$\therefore$  All three methods give the same estimate  $n_e$ .**



# Temperature and Debye Length

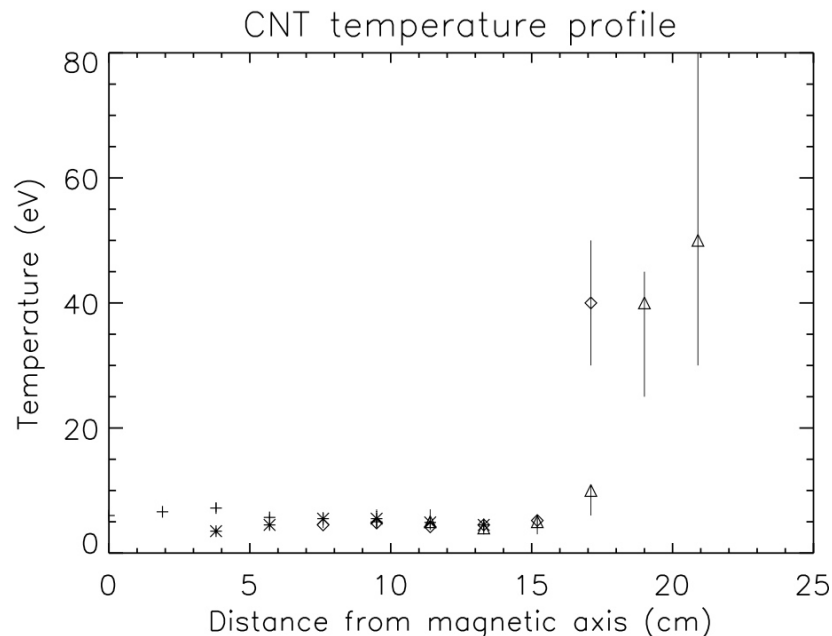
For  $-200$  V emitter bias,  $B = 0.02$  T and  $P_n = 5 \times 10^{-9}$  Torr:

- Measured  $T_e$  as 3~6 eV
- The  $T_e$  profile was flat through most of the confining region.
- Using  $n_e \sim 10^{12} \text{m}^{-3}$ :

$$\rightarrow \lambda_D \sim 2 \text{ cm}$$

$$\therefore \lambda_D/a \ll 1 :$$

**We have a plasma!**



## Emitter bias optimization:

- $n_e$  has linear dependence on emitter bias.
- $T_e$  seems to have minimum.  
→ Optimized emitter bias seems to be around  $-100$  V.
- What sets  $T_e$ ?





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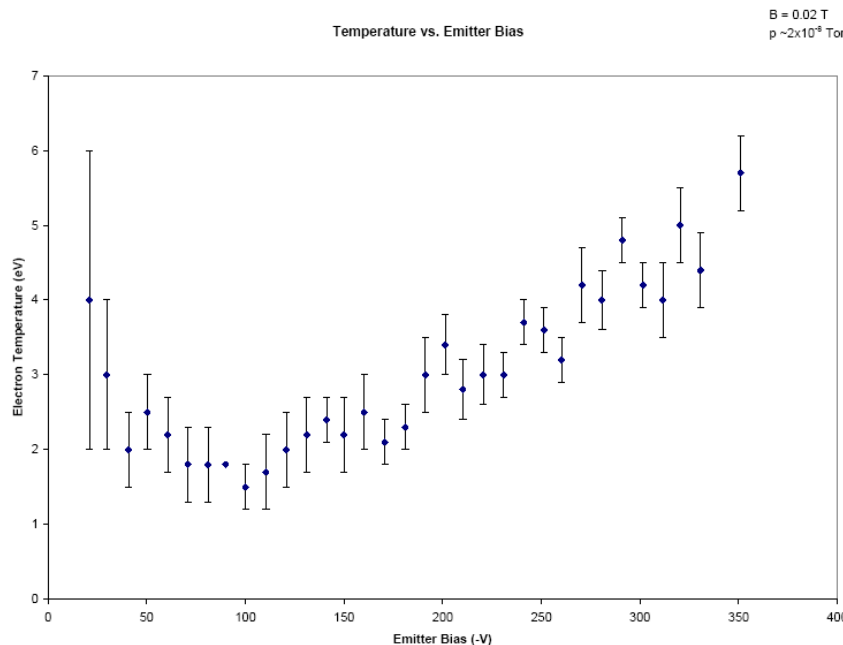
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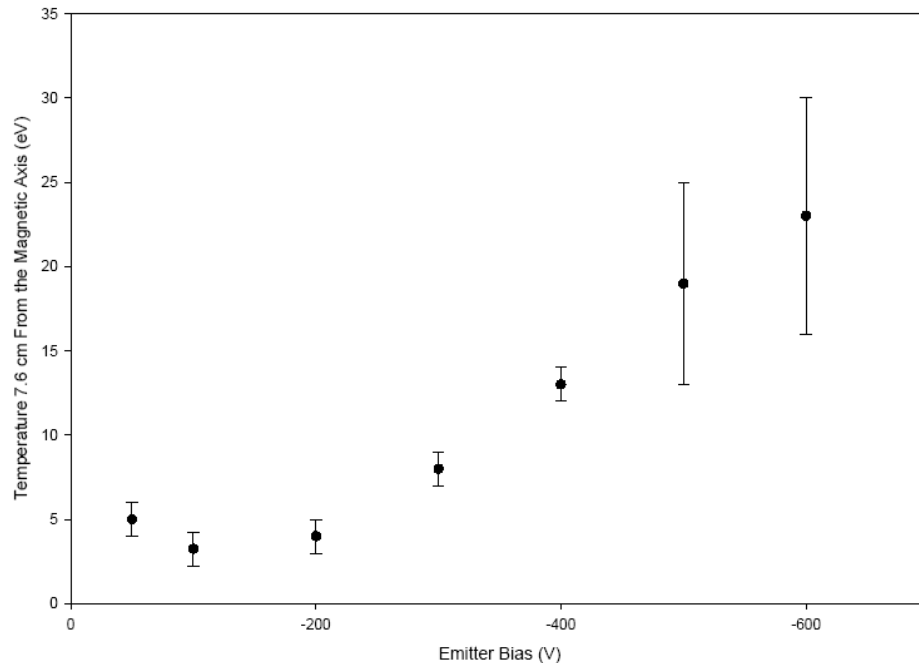
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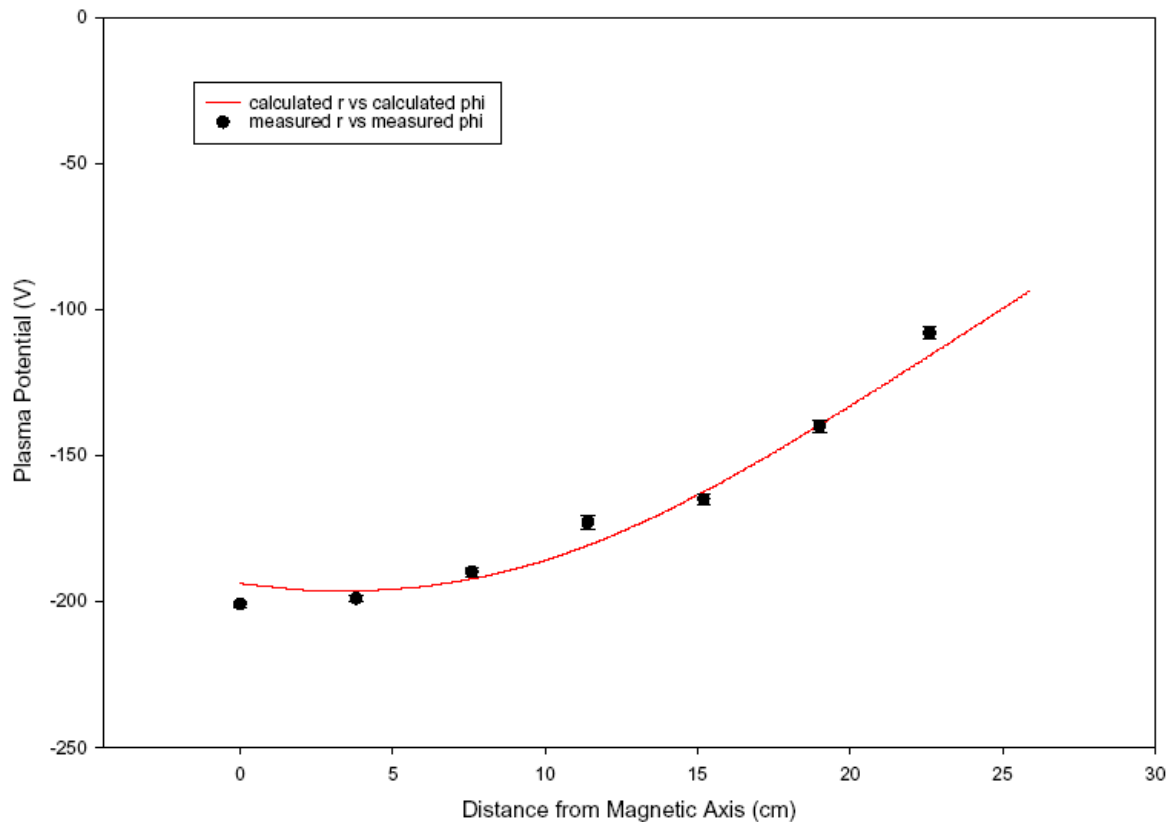
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# A Profile Measurement

- The 3-D equilibrium code was used to perform a fit on the potential profile.
  - Use measured temperature (flat profile at 5 eV).
  - Assume parabolic  $N(\Psi)$  profile.
  - Adjust  $N$  until best fit with measured potential profile.



This is consistent with:

$$\nabla^2 \phi = \frac{e}{\epsilon_0} N(\psi) \exp\left(\frac{e\phi}{T_e(\psi)}\right)$$

**Measurements are ongoing...**



# Electron Confinement Time

## Measurement of the confinement time, $\tau_c$ :

- The source rate of electrons emitted from the filament is  $S = I/e$ .
- The loss rate of electrons from the confining region is  $L = N/\tau_c$ .
- In steady-state,  $S = L$ .
  - $\tau_c = eN/I$

**We have measured  $\tau_c \sim 20$  ms.**

## A comparison of $\tau_c$ to other relevant time scales:

- Parallel force balance  $\sim 10 \mu\text{s}$
- Time for an electron to escape at  $E \times B$  velocity  $\sim 20 \mu\text{s}$
- Time for an electron to  $\nabla B$  drift out  $\sim 300 \mu\text{s}$

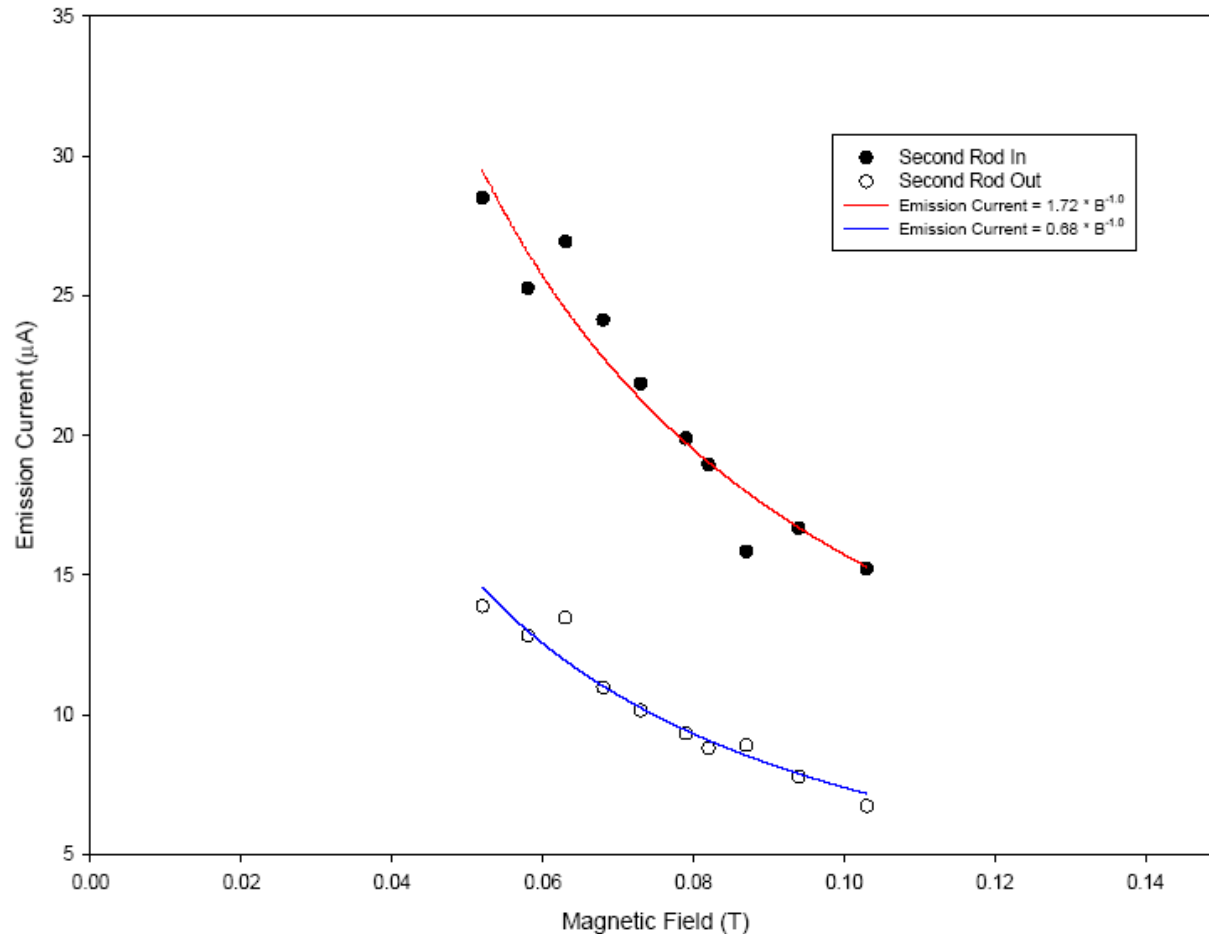
**$\therefore$  Macroscopically stable equilibrium has been observed but...**

- Expected confinement time scaling:  $(a/\lambda_D)^4 \tau_e \sim 600$  s

**...confinement times are not as long as expected.**



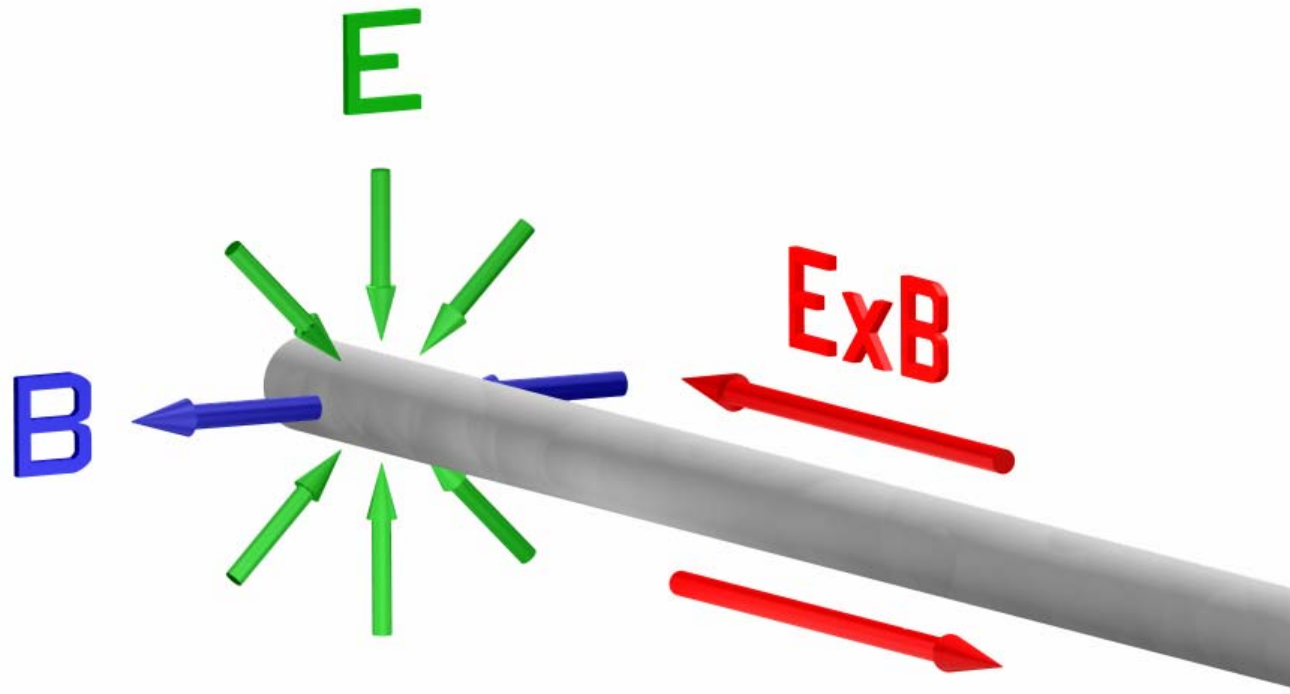
# Measurement of Effect of Rods on Confinement



- Shorter confinement time (higher emission current) with the extra rod in.
- Emission scales as  $1/B$  ( $V_{\text{ExB}} \sim E/B$ )
  - (Bohm scaling?).
- A retracting emitter is now under construction...



## Bulk $E \times B$ Flows Along Rod?



- The insulating rod is a significant drive for radial particle transport.
  - The rod charges up negatively (electric field radial from rod).
  - The resulting local electric field crossed with the magnetic field drives inward and outward flows.
  - The net flow is outward.



# Summary

- CNT is a university scale experiment designed to non-neutral and partially neutralized plasmas on magnetic surfaces.
  - The first CNT experiments are with pure electron plasmas.
- $\lambda_D/a \ll 1$  has been achieved.
- Profile measurements are consistent with theoretical equilibrium predictions.
- ~20 ms confinement times have been measured.
  - Confinement time is presently limited by rods.
- Future experiments will utilize less perturbative emitters and diagnostics.

